

ODE

First Order ODE

Linear

1. $y' + y = e^t + 11$

2. $y' \cos(x) + y \sin(x) = 1$

3. $y' \cos(x) = y \sin(x) + \sin(2x)$

4. $y' - 2xy = e^{x^2}$

5. $y' + y = (x + 1)^2, y(0) = 0$

6. $2y + (x + 1) \frac{dy}{dx} = 3x + 3, y(0) = 3$

7. $y' - 3y = 3e^{4t}, y(0) = 5$

8. $y' = \frac{1}{3}y - e^{-4x}, y(0) = 7$

9. $y' = x + y, y(0) = 1$

10. $x \frac{dy}{dx} + y = x, y(1) = 1$

Answers

ODE

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Linear

$$1. y = \frac{e^t}{2} + 11 + \frac{c_1}{e^t}$$

$$2. y = \frac{\tan(x)}{\sec(x)} + \frac{c_1}{\sec(x)}$$

$$3. y = -\frac{\cos(2x)}{2\cos(x)} + \frac{c_1}{\cos(x)}$$

$$4. y = e^{x^2} x + c_1 e^{x^2}$$

$$5. y = x^2 + 1 - \frac{1}{e^x}$$

$$6. y = \frac{x^3}{x^2 + 2x + 1} + \frac{3x^2}{x^2 + 2x + 1} + \frac{3x}{x^2 + 2x + 1} + \frac{3}{x^2 + 2x + 1}$$

$$7. y = 3e^{4t} + 2e^{3t}$$

$$8. y = \frac{3}{13e^{4x}} + \frac{88}{13} e^{\frac{x}{3}}$$

$$9. y = -x - 1 + 2e^x$$

$$10. y = \frac{x}{2} + \frac{1}{2x}$$